ϵ_t is independent of ϵ_{t-1} (by definition). Y_{t-1} depends on ϵ_{t-1}, ϵ_{t-2}, and previous random variables, all of which are independent of ϵ_t. The covariance depends only on the variance of ϵ_t, which is σ^2_{ε}.