MS Module 12 ANOVA unequal group sizes practice exam questions
(The attached PDF file has better formatting.)
An experiment has three groups; the number of observations per group and the group means are

|  | size | mean |
| :--- | :---: | :---: |
| group 1 | 21 | 51 |
| group 2 | 34 | 76 |
| group 3 | 31 | 70 |

- The sum of the squares of the observations is 590,645
- The observations have normal distributions in each group, and the variance in each group is the same.
- The null hypothesis is that the means of the groups are equal: $\mathrm{H}_{0}: \mu_{1}=\mu_{2}=\mu_{3}\left[\mu_{\mathrm{j}}=\right.$ mean of Group J]


## Question 12.1: Square of sum of observations

What is the square of the sum of all the observations, or $\mathrm{x}_{.2}$ ?
Answer 12.1: $(21 \times 51+34 \times 76+31 \times 70)^{2}=33,930,625$
(square of the sum of the observations $\left.=(\Sigma \text { (observations in group } \times \text { mean of group) })^{2}\right)$

Question 12.2: Correction factor
What is the correction factor for SST and SSTr?
Answer 12.2: 33,930,625 $/(21+34+31)=394,542.15$
(correction factor $=$ square of the sum of the observations / total observations)

Question 12.3: Total sum of squares

What is SST, the total sum of squares?
Answer 12.3: 590,645-394,542.15 = 196,102.85
(total sum of squares $=$ sum of squares of observations - correction factor)

Question 12.4: Treatment sums of squares
What is SSTr, the treatment sum of squares?
Answer 12.4: $\left(21 \times 51^{2}+34 \times 76^{2}+31 \times 70^{2}\right)-394,542.15=8,362.85$
(total sum of squares $=\Sigma$ (observations by group $\times$ square of mean by group) - correction factor)

Question 12.5: Error sum of squares
What is SSE, the error sum of squares?
Answer 12.5: 196,102.85-8,362.85 = 187,740.00
(error sum of squares $=$ total sum of squares - treatment sums of squares)

Question 12.6: Total degrees of freedom
What are the total degrees of freedom?
Answer 12.6: $(21+34+31-1)=85$
(total degrees of freedom $=$ number of observations -1 )

Question 12.7: Degrees of freedom for the groups
What are the degrees of freedom for the groups?
Answer 12.7: 3-1 = 2

Question 12.8: Degrees of freedom for the error sum of squares
What are the degrees of freedom for the error sum of squares (SSE)?
Answer 12.8: $85-2=83$

Question 12.9: Mean squared deviation for the groups
What is MSTr, the mean squared deviation for the groups (treatment mean square)?
Answer 12.9: 8,362.85 / $2=4,181.425$

Question 12.10: Mean squared error
What is MSE, the mean squared error?
Answer 12.10: 187,740.00 / $83=2,261.928$

Question 12.11: F value
What is the $F$ value for testing the null hypothesis?
Answer 12.11: 4,181.425 / 2,261.928 = 1.849

