Macro Module 3 Cobb-Douglas production function practice exam questions

An economy has a Cobb-Douglas production function: $Y = AK^{\alpha} L^{(1-\alpha)}$.

A is the technology level, K is capital; L is labor; and Y is income.

- In 20X1, the technology level A is 143, capital K = 236, labor L = 458, income Y = 8,808
- In 20X2, the technology level A is 149.05, capital K = 248.74, labor L = 472.98, income Y = 9,620.56
- In 20X3, the technology level A is 155.59, capital K = 263.12, labor L = 490.71

Question 3.1: Percentage changes

What are the percentage changes for A, K, L, and Y from 20X1 to 20X2?

Answer 3.1: percentage change = (20X2 value – 20X1 value) / 20X1 value:

- technology level (A): (149.05 143) / 143 = 4.23%
- capital (K): (248.74 236) / 236 = 5.40%
- labor (L): (472.98 458) / 458 = 3.27%
- income (Y): (9,620.56 8,808) / 8,808 = 9.2253%

Question 3.2: a parameter (exponent of capital)

What is the α parameter (the exponent of capital) of the Cobb-Douglas production function?

Answer 3.2: $4.23\% + \alpha \times 5.40\% + (1 - \alpha) \times 3.27\% = 9.2253\% \Rightarrow \alpha \times (5.40\% - 3.27\%) = (9.2253\% - 3.27\% - 4.23\%) \Rightarrow \alpha = (9.2253\% - 3.27\% - 4.23\%) / (5.40\% - 3.27\%) = 81.00\%$

Question 3.3: Elasticity of income with respect to capital

What is the elasticity of income with respect to capital?

Answer 3.3: 81% (= α)

Question 3.4: Elasticity of income with respect to labor

What is the elasticity of income with respect to labor?

Answer 3.4: 1 – 81% = 19%

Question 3.5: Percentage changes for factors of production

What are the percentage changes for A, K, and L from 20X2 to 20X3?

Answer 3.5: percentage change = (20X3 value – 20X2 value) / 20X2 value:

- technology level (A): (155.59 149.05) / 149.05 = 4.39%
- capital (K): (263.12 248.74) / 248.74 = 5.78%
- labor (L): (490.71 472.98) / 472.98 = 3.75%

Question 3.6: Percentage change for income

What is the percentage change for Y from 20X2 to 20X3?

Answer 3.6: 4.39% + 81% × 5.78% + 19% × 3.75% = 9.7843%

Question 3.7: Income

What is income (Y) in 20X3?

Answer 3.7: 9,620.56 × (1 + 9.7843%) = 10,561.86