MS Module 23 Balance principle additive model practice exam questions
(The attached PDF file has better formatting.)
[The practice problems in the 24 modules explain the statistical procedures; the practice exam questions in this thread shows what you will be asked on the final exam.]

The mean values and the number of observations in each cell of a $2 \times 2$ classification table are

| Means | Column 1 | Column 2 | Observations | Column 1 | Column 2 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Row 1 | 79 | 58 | Row 1 | 14 | 15 |
| Row 2 | 31 | 12 | Row 2 | 11 | 18 |

Illustration: The cell in row 1 column 1 has a mean of 79 from a sample of 14 observations.
An actuary is setting class relativities for insurance pricing using an additive model and the balance principle. The mean value of the cell with row $(\mathrm{j})$ and column $(\mathrm{k})=$ base rate + row relativity $(\mathrm{j})+$ column relativity $(\mathrm{k})$.

The base rate is 10 , and the initial column relativities are 18 for Column 1 and 0 for Column 2.

Question 23.1: Balance principle additive model implied relativity row 1
What is the implied relativity for Row 1 , using the initial relativities by column?
Answer 23.1: $(79 \times 14+58 \times 15-(14 \times(10+18)+15 \times(10+0))) /(14+15)=49.448$
(implied relativity for row 1 = observed value for row 1 - expected value for row 1 with no relativity)

Question 23.2: Balance principle additive model implied relativity row 2
What is the implied relativity for Row 2, using the initial relativities by column?
Answer 23.2: $(31 \times 11+12 \times 18-(11 \times(10+18)+18 \times(10+0))) /(11+18)=2.379$
(implied relativity for row 2 = observed value for row 2 - expected value for row 2 with no relativity)

Question 23.3: Balance principle additive model implied relativity column 1
What is the implied relativity for Column 1 , using the computed relativities by row?
Answer 23.3: $(79 \times 14+31 \times 11-(14 \times(10+49.448)+11 \times(10+2.379))) /(14+11)=19.142$
(implied relativity for column 1 = observed value for column 1 - expected value for column 1 with no relativity)

Question 23.4: Balance principle additive model implied relativity column 2
What is the implied relativity for Column 2, using the computed relativities by row?

Answer 23.4: $(58 \times 15+12 \times 18-(15 \times(10+49.448)+18 \times(10+2.379))) /(15+18)=-0.865$
(implied relativity for column 2 = observed value for column $2-$ expected value for column 2 with no relativity)

