

Corffin, Mod 19: Debt tax shields and adjusted present value sample exam problem

Exercise 19.1: Debt tax shields and adjusted present value

A firm undertakes a one year project on January 1 with the following attributes:

- ! The initial investment is 2,016.
- ! The project provides an expected return of 2,244 at the end of the year (December 31).
  
- ! The opportunity cost of capital is 9.4% *per annum*.
- ! The return on debt  $r_D$  is 6.3% *per annum*.
- ! The debt to value ratio (D/V) is 34.2%.
- ! The corporate tax rate is 28.4%.

- A. What is the base case net present value of the project?
- B. What is the present value of the debt tax shield?
- C. What is the adjusted present value of the project?

*Part A:* The base case net present value of the project is the NPV of the cash flows at the opportunity cost of capital, ignoring the debt financing:

$$- 2,016 + 2,244 / 1.094 = 35.19$$

*Part B:* The debt is the initial investment times the debt to value ratio:

$$2,016 \times 34.2\% = 689.47$$

The interest payment is the debt times the return on debt:

$$2,016 \times 34.2\% \times 6.3\% = 43.44$$

The nominal value of the debt tax shield is the interest payment times the corporate tax rate:

$$2,016 \times 34.2\% \times 6.3\% \times 28.4\% = 12.34$$

The present value of the debt tax shield is the nominal value discounted at the return on debt.

$$2,016 \times 34.2\% \times 6.3\% \times 28.4\% / (1.063) = 11.60$$

*Part C:* The adjusted present value of the project is the base case net present value plus the present value of the debt tax shield:

$$35.19 + 11.60 = 46.79$$